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## INSTRUCTIONS: <br> - OPEN BOOK/OPEN NOTES/COMPUTERS ALLOWED

- TIME: 3 HOURS
- WRITE YOUR NAME AND ID NUMBER IN THE SPACE PROVIDED ABOVE.
- WRITE YOUR ANSWERS ON THE QUESTION SHEET.
- THE SCRATCH BOOKLET WILL NOT BE CONSIDERED IN GRADING.
- WRITE COMMENTS NEXT TO YOUR MIPS INSTRUCTIONS.
- PAGE 2 LISTS SOME COMMON MIPS INSTRUCTIONS YOU CAN USE
- BE AS CLEAR AND AS NEAT AS POSSIBLE.
- WRITE DOWN ANY ASSUMPTIONS YOU USE IN SOLVING ANY PROBLEM.

| PROBLEM | MAX POINTS | GRADE |
| :---: | :---: | :---: |
| 1 | 20 |  |
| 2 | 20 |  |
| 3 | 20 |  |
| 4 | 25 |  |
| 5 | 20 |  |
| 6 | 20 |  |
| 7 | 10 |  |
| 8 | 25 |  |
| TOTAL | 160 |  |

## MIPS Instructions

These are some of the most common MIPS instructions and pseudo-instructions, and should be all you need. However, you are free to use any valid MIPS instructions or pseudo-instruction in your programs.

| Category | Example Instruction |  | Meaning |
| :---: | :---: | :---: | :---: |
| Arithmetic | rem <br> div <br> mul <br> addi <br> sub <br> add <br> addu <br> addiu | $\$ t 0$, $\$ t 1$, $\$ t 2$ <br> $\$ t 0$, $\$ t 1$, $\$ t 2$ <br> $\$ t 0$, $\$ t 1$, $\$ t 2$ <br> $\$ t 0$, $\$ t 1$, 100 <br> $\$ t 0$, $\$ t 1$, $\$ t 2$ <br> $\$ t 0$, $\$ t 1$, $\$ t 2$ <br> $\$ t 0$, $\$ t 1$, $\$ t 2$ <br> $\$ t 0$, $\$ t 1$, 100 | $\begin{aligned} & \$ t 0=\$ t 1 \text { mod } \$ t 2 \\ & \$ t 0=\$ t 1-\$ t 2 \\ & \$ t 0=\$ t 1 \times \$ t 2 \\ & \$ t 0=\$ t 1+100 \\ & \$ t 0=\$ t 1-\$ t 2 \\ & \$ t 0=\$ t 1+\$ t 2 \\ & \$ t 0=\$ t 1+\$ t 2 \quad \# \text { unsigned } \\ & \$ t 0=\$ t 1+100 \quad \text { \# unsigned } \end{aligned}$ |
| Logic | or <br> and <br> nor <br> xor | $\$ t 0$, $\$ t 1$, $\$ t 2$ <br> $\$ t 0$, $\$ t 1$, $\$ t 2$ <br> $\$ t 0$, $\$ t 1$, $\$ t 2$ <br> $\$ t 0$, $\$ t 1$, $\$ t 2$ | $\begin{aligned} & \$ t 0=\$ t 1 \text { or } \$ t 2 \\ & \$ t 0=\$ t 1 \text { and } \$ t 2 \\ & \$ t 0=\$ t 1 \text { nor } \$ t 2 \\ & \$ t 0=\$ t 1 \text { xor } \$ t 2 \end{aligned}$ |
| Register Setting | li move | $\begin{array}{ll} \$ t 0, & 100 \\ \$ t 0, & \$ t 1 \end{array}$ | $\begin{aligned} & \$ t 0=100 \\ & \$ t 0=\$ t 1 \end{aligned}$ |
| Data Transfer | $\begin{aligned} & \hline s w \\ & \text { lw } \\ & 1 . s \\ & s . s \\ & 1 . d \\ & \text { s.d } \end{aligned}$ | $\$ t 0$, $100(\$ t 1)$ <br> $\$ t 0$, $100(\$ t 1)$ <br> $\$ f 0$, $100(\$ t 1)$ <br> $\$ f 0$, $100(\$ t 1)$ <br> $\$ f 0$, $100(\$ t 1)$ <br> $\$ f 0$, $100(\$ t 1)$ | $\begin{aligned} & \text { Mem }[100+\$ t 1]=\$ t 0 \\ & \$ t 0=\operatorname{Mem}[100+\$ t 1] \\ & \$ f 0=\operatorname{Mem}[100+\$ t 1] \\ & \operatorname{Mem}[100+\$ t 1]=\$ f 0 \\ & \$ f 0=\operatorname{Mem}[100+\$ t 1], \quad \$ f 1=\operatorname{Mem}[104+\$ t 1] \\ & \operatorname{Mem}[100+\$ t 1]=\$ f 0, \operatorname{Mem}[104+\$ t 1]=\$ f 1 \end{aligned}$ |
| Branch | blt <br> ble <br> bgt <br> bge <br> bne <br> beq | \$t0, $\$ t 1$, Label \$t0, $\$ t 1$, Label \$t0, $\$ t 1$, Label \$t0, $\$ t 1$, Label \$t0, $\$ t 1$, Label \$t0, \$t1, Label | if $(\$ t 0<\$ t 1)$ go to Label if $(\$ t 0 \leq \$ t 1)$ go to Label if $(\$ t 0>\$ t 1)$ go to Label if $(\$ t 0 \geq \$ t 1)$ go to Label if $(\$ t 0 \neq \$ t 1)$ go to Label if $(\$ t 0=\$ t 1)$ go to Label |
| Set | slti <br> sltiu <br> slt <br> sltu | $\$ t 0$, $\$ t 1$, 100 <br> $\$ t 0$, $\$ t 1$, 100 <br> $\$ t 0$, $\$ t 1$, $\$ t 2$ <br> $\$ t 0$, $\$ t 1$, $\$ t 2$ | if (\$t1 < 100) then $\$ \mathrm{tO}=1$ else $\$ \mathrm{tO}=0$ <br> if ( $\$ \mathrm{t} 1<100$ ) then $\$ \mathrm{tO}=1$ else $\$ \mathrm{tO}=0$ <br> if ( $\$ \mathrm{t} 1<\$ \mathrm{t} 2$ ) then $\$ \mathrm{tO}=1$ else $\$ \mathrm{tO}=0$ <br> if ( $\$ \mathrm{t} 1<\$ \mathrm{t} 2$ ) then $\$ \mathrm{t0}=1$ else $\$ \mathrm{t} 0=0$ |
| Jump | $\begin{aligned} & \text { jal } \\ & \text { jr } \\ & \text { j } \end{aligned}$ | Label \$ra Label | \$ra = PC + 4; go to Label go to address in \$ra go to Label |

## Problem 1: General Questions [20 points]

a) Let the number $\boldsymbol{y}=0 \times 4$ CDD 0000 represent a single precision IEEE 754 number. Represent $\boldsymbol{y}$ in doubleprecision IEEE 754 format. Write your result in hexadecimal [5 points]

## Answer:

b) A frequently used instruction in multimedia applications is the swap $\$ \mathrm{t} 1, \$ \mathrm{t} 2$ instruction which swaps the upper and lower16 bits of $\$ \mathrm{t} 2$ and stores the result in $\mathbf{\$ t 1}$. Implement the swap instruction in MIPS using no more than 3 instructions (no pseudo-instructions allowed). [5 points]

Answer:
c) Assume variables $\mathbf{u}$ and $\mathbf{v}$ are two integers represented in 2's complement notation and that $\mathbf{v}$ is positive. Implement the following $C$ expression using exactly three instructions (no pseudo-instructions): [5 points]

```
if ( 0 \leq u < v ) u = u + v;
```


## Answer:

d) Represent the decimal number $-8.875 \times 2^{3}$ in IEEE 754 single precision format. Give your result in hexadecimal format. [5 points]

## Answer:

## Problem 2: Set-Less-Than [20 points]

Suppose the instructions slt, sltu, slti, sltiu were removed from the MIPS instruction set. Show how to perform slt $\mathbf{\$ s} \mathbf{0}, \mathbf{s} \mathbf{s} \mathbf{, \$ s} \mathbf{s}$ using the modified instruction set in which slt is not available (no pseudo-instructions allowed). Beware to account for overflow.

## Solution:

## Problem 3: Understanding MIPS Programs [20 points]

Translate the function AMD into C. You should follow all MIPS function conventions. Your code should be as concise as possible, without any gotos or pointers [15 points]. Describe what the function does. [ 5 points]

| AMD : | $\begin{array}{lll} \text { li } \$ t 0, & 0 \\ \text { li } \$ t 1, & 0 \\ \text { li } \$ t 2, & 0 \times 3 f f f f f f f \end{array}$ |
| :---: | :---: |
| ALPHA : | ```bge $t0, $a1, POWERPC mul $t3, $t0, 4 add $t3, $a0, $t3 lw $t3, 0($t3) ble $t3, $t1, PS2 move $t1, $t3``` |
| PS2 : | bge \$t3, \$t2, SPARC move \$t2, \$t3 |
| SPARC : | $\begin{aligned} & \text { addi } \$ t 0, \$ t 0,1 \\ & \text { j ALPHA } \end{aligned}$ |
| POWERPC: | ```sw $t1, 0($a2) sw $t2, 0($a3) jr $ra``` |

## Solution:

## Problem 4: MIPS Programming [25 points]

The goal of this problem is to write a MIPS function flipimage which flips an image horizontally. For example, a simple image is shown on the left, and its flip is shown on the right.


A picture is composed of individual dots, or pixels, each of which will be represented by a single byte. The entire two-dimensional image is then stored in memory row by row. For example, we can store a $4 \times 6$ picture in memory starting at address 1000 as follows:

- The first row (consisting of 6 pixels) is stored at addresses 1000-1005.
- The second row is stored at addresses 1006-1011.
- The third row is stored at 1012-1017
- The last row is stored at addresses 1018-1023.
a) Write a MIPS function fliprow to flip a single row of pixels. The function has two arguments, passed in $\$ \mathrm{aO}$ and $\$ \mathrm{a} 1$ : the address of the row and the number of pixels in that row. There is no return value. Be sure to follow all MIPS calling conventions. [ $\mathbf{1 0}$ points]

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b) Using the fliprow function, you should now be able to write flipimage. The arguments will be:

- The memory address where the image is stored
- The number of rows in the image
- The number of columns in the image

Again, there is no return value, and you should follow normal MIPS calling conventions. [15 points]

| MIPS Code | Comments |
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## Problem 5: Recursive Functions [20 points]

Compile the following function into MIPS. You must follow all MIPS conventions. Add comments to your code. You will be graded on the efficiency of your code.

```
int function(int x) {
    if (x == 0)
    return 0;
    int temp = x & 1;
    return temp + function(x >> 1);
}
```

| MIPS Code | Comments |
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## Problem 6: Maximum [20 points]

Implement the instruction max $\$ \mathrm{t} 1, \mathbf{\$ t 2}, \mathbf{\$ t 3}$ in MIPS, which returns the maximum of $\mathbf{\$ t 2}$ and $\$ \mathrm{t} 3$ in $\$ \mathrm{t} 1$, without using any conditional branch instructions (beq, bne). Also, you are not allowed to use pseudoinstructions.

## Solution:

## Problem 7: Speedup [10 points]

We are interested in determining the speedup ( $\boldsymbol{S}$ ) gained from a certain improvement made to enhance a computer. The improvement targets two classes of instructions which roughly constitute a fraction $\boldsymbol{p}_{1}$ and $\boldsymbol{p}_{2}$, respectively, of the overall instructions used. The first class of instructions runs $\boldsymbol{x}_{1}$ times faster with the improvement, while the second runs $\boldsymbol{x}_{2}$. times faster. Determine $\boldsymbol{S}$ in terms of $\boldsymbol{p}_{1}, \boldsymbol{p}_{2} . \boldsymbol{x}_{1}, \boldsymbol{x}_{2}$.

## Solution:

## Problem 8: Square Function [20 points]

Let $\mathbf{A}$ be a $30 \times 20$ array of single-precision floating point numbers whose base address in memory is stored in register $\mathbf{\$ a 0}$. The elements of $\mathbf{A}$ are stored in column-major form in memory. Write a function in MIPS that squares the elements of $\mathbf{A}$ and stores the resulting array at memory address $\$ \mathrm{a} 1$ in column-major form. Be sure to follow all MIPS calling conventions. Comment your code.

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